

# Master of Engineering Subject Code: 3720820 MULTIBODY DYNAMICS SEMESTER: II

# **Type of course:** Program Elective

# **Prerequisite:** Zeal to learn the subject

**Rationale:**This course reviews and reinforces the student's understanding Kinematics and Dynamics of multibody systems with immediate application to the dynamics of systems of rigid bodies. The course will place equal emphasis on gaining both an analytical understanding and insight/intuition on the subject.

# **Teaching and Examination Scheme:**

Teaching Scheme			Credits	Examination Marks				Total
L	Т	Р	С	Theory Marks		Practical Marks		Marks
				ESE (E)	PA (M)	ESE (V)	PA (I)	
3	0	2	4	70	30	30	20	150

# **Contents:**

Sr.	Торіс				
No	1 opro				
1	Basic concepts in 3-D rigid-body mechanics				
	Degrees-of-freedom;Rigid body vs flexible body; Spatial kinematics (3-D rotation				
	transformations); Euler theorem, rotation parameterization, Rodriguez formula;	11			
	Moments and products of inertia; Newton-Euler equations of motion; Lagrange				
	Equation; Generalized forces.				
2	Inter-connected rigid bodies				
	Kinematic pairs (joints) with classification of constraints; holonomic and non-	ſ			
	holonomic constraints; Springs, dampers, actuators and controllers with brief	6			
	introduction of controls theory.				
3	Formulation of equations of motion for inter-connected bodies				
	Relative coordinates, generalized coordinates, Cartesian co-ordinates ; Lagrange' s				
	equations and other approaches; Differential equations (ODE) and differential algebraic				
	equations (DAE); Co-ordinate partitioning and Lagrange multipliers; Types of analyses	11			
	(kinematic, static, quasi-static, kineto-static, dynamic and linear dynamic).				
4	Application of numerical methods				
	NR method, Jacobian, ODE integrators (Euler methods and Implicit methods); Stability,				
	accuracy and Dahlquist's tradeoff criteria; Stiffness and damping - physical vs	7			
	numerical; Lock-up, bifurcation and singularities.				
5	Flexible Multibody Systems	7			
	Dynamic analyses using classical approximation, FEM	1			



# **GUJARAT TECHNOLOGICAL UNIVERSITY**

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#### **References Books:**

- 1. Computational dynamics, Shabana A. A., John Wiley & Sons.
- 2. Dynamics of Multibody Systems, Roberson R. E., and Richard S., Springer-Verlag.
- 3. Dynamics of Multibody Systems, Shabana A. A., Cambridge University press.
- 4. Flexible Multibody Dynamics, Bauchau O. A., Vol. 176. Springer.
- 5. Dynamics and Balancing of Multibody Systems, Chaudhary H., and S K Saha. Springer.

#### **Course Outcome:**

After learning the course

Sr. No.	Course Outcome	Percentage weightage
CO-1	Students will be able to apply basic particle dynamics and 2-dimensional rigid body mechanics to 3-dimensional rigid bodies.	35%
CO-2	Students will be able to analyse interconnected bodies in a multi-body system.	35%
CO-3	Students will be able to use numerical methods for the analysis of multi- body system.	30%

## List of Experiments:

- 1. Kinematics of a planar open-loop system using MATLAB/Scilab
- 2. Inverse dynamics of planar open-loop systems using MATLAB/Scilab
- 3. Forward dynamics of planar open-loop systems using MATLAB/Scilab
- 4. Kinematics of a planar closed-loop system using MATLAB/Scilab
- 5. Inverse dynamics of planar closed-loop systems using MATLAB/Scilab
- 6. Forward dynamics of planar closed-loop systems using MATLAB/Scilab
- 7. Kinematics of a spatial closed-loop system using MATLAB/Scilab
- 8. Inverse dynamics of spatial closed-loop systems using MATLAB/Scilab
- 9. Forward dynamics of spatial closed-loop systems using MATLAB/Scilab
- 10. Modellingand analysis of multibody systems using MBD software.

#### **Major Equipment:**

- 1. Computational facility and Matlab / Scilab.
- 2. Mechanism analysis software.

## List of Open Source Software/learning website:

Scilab Software